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## **Verification of Partial Properties**

### **Introduction**

*Section 3.1 of "Correctness Preserving Transformation"  
ESPRIT Project 2304 LOTOSPHERE*

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## Section 3.1

### Introduction

#### 3.1.1 The meaning of "Partial Properties"

By "partial property" we mean a partial representation of the behaviour of a system, which abstracts from details which are considered as irrelevant for that representation. The main purpose of this chapter is to define notions of correctness given by partial properties, in order to complement the usual notion of correctness as an equivalence of two complete specifications, studying in detail the possible roles, advantages and application techniques of partial properties in the context of correctness preserving transformations. This concept is opposed to that of a "total" representation of the behaviour of the system, such as that considered, for instance, when we want to verify the equivalence of a given specification and its implementation. In this sense, the other chapters of this document on Correctness Preserving Transformations are mostly concerned with the preservation of "total" properties.

##### Simple classes of partial properties

As simple instances of partial properties, we can first mention the structural properties of the specification, like the style in which the specification is written (constraint-oriented, state-oriented,...), or particular views on the specification, intended as restrictions of its sort (the set of its visible gates).

It is however more interesting to consider semantic properties, which can be imposed as requirements on the specification. We may, for instance, refer to the classical distinction of partial properties into *safety* (something bad never happens) and *liveness* properties (something good eventually happens) [L83] or to the finer classification given in [MP89], in which liveness properties are furtherly divided in finer classes, like *termination* (a good thing happens in some state of the computation), *persistence* (something good happens in all, except for finitely many, states of the computation), *recurrence* (something good happens in infinitely many states of the computation), or *response* (the occurrence of an event always triggers another event). We can also identify other, generally useful, classes of properties such as *potentiality* (there is the possibility that something will happen).

### Some examples of partial properties

Let us consider the following natural language specification of the properties of a database system:

- 1) A user cannot access the database if he/she has not correctly typed his/her password.
- 2) Whenever a logged user queries the database, he/she eventually gets a reply from it.
- 3) The database system may refuse the service to a user (e.g. due to its own capacity limits).

We can recognize the first point as a safety property, the second as a response property (also a liveness property), and the third as a potentiality property.

Other useful properties can often be considered as belonging to one of the above classes. For example the insensitiveness of a specification to the underlying form of communication (synchronous or asynchronous) can be seen as a response property: every sent message will eventually arrive at destination.

## 3.1.2. Formalisms to express partial properties

### Temporal Logic

Temporal Logic [MP81, P81, L83] has been long recognized as a valid tool to specify and verify properties of concurrent systems, working at a higher level of abstraction with respect to the constructive formalisms used for specifying concurrent systems such as LOTOS.

Formulae in temporal logic, do not only express the truth of a certain statement, but its truth relative to a point in time, using connectives such as "next", "always", "eventually", "until", and so on. In this way, we can express statements of systems which evolve in time.

For example, the statement seen above: "Whenever a logged user queries the database, he/she eventually gets a reply from it", can be expressed by the temporal logic formula:

always ( query implies eventually (reply))

where query and reply are predicates which are true if the events of querying the database or of getting a reply from it, occur.

An important distinction of the possible temporal logic definitions is made on the basis of the structure of time chosen. If the structure of time considered is linear (each moment has exactly one future) we have a "linear temporal logic". If the structure of time is "branching" (every moment may have more than one future) we have a "branching temporal logic". This distinction is important for the expression of properties: safety and liveness properties are expressed in linear temporal logic, but potentiality properties can be expressed only by branching temporal logic.

The question of the expressibility of fairness properties in branching temporal logic has, in the past, given rise to considerable discussion. [L81, EH86].

### Partial Process Specifications

Another way to express partial properties is by partial process specifications, in a language which can be either LOTOS itself or an extended "annotated" version of it. One must provide in addition *procedures of reductions* to be applied to the (concrete) system under analysis, before it is compared with the partial specification. The idea here is twofold: first, only certain aspects

of the behaviours are focussed on, discarding others, and thus the process, seen from a certain angle, is mapped to the desired property expressed as another process; second, complementary pertinent items of information, increasing practical expressivity, can be figured explicitly in an appropriate form both in the specification and in the process reduction, thus providing further insights.

As an instance of the first case, the theory of "process abstraction" was devised in [B85]. A syntax allowing the definition of "abstract actions", as in databases transactions for instance, is introduced in that paper. Following a linear time philosophy, a search is then made for paths of behaviours in the process; the result is an "abstract transition system", usually much simpler to comprehend. We shall call *experiments* these sequences of behaviours which belong to a given abstract action. A fairly common use of abstract actions is refutation: a *Positive* set of experiments is introduced, which intuitively should lead to well-identified configurations of the system. They are supplemented by another set *Negative* - those which should not be possible. The presence of the second type of abstract actions in the reduced system is thus highly indicative, since they identify locations (or configurations) where faulty behaviours may occur. This particular verification could be summed up in logical terms:

always (no experiment from Negative after an experiment from Positive),  
and bears strong links with the theory of testing. This approach was exemplified in [BRSV89].

As an instance of the second case, divergence predicates can carry information to the user on invisible aspects of the processes, such as livelock states.

Connections between temporal logics and reduction can be drawn: Propositional Dynamic Logic [P79] uses abstract actions as parameters to the logical modalities, so that  $[R]f$  means "always  $f$  after any experiment belonging to  $R$ ". Proving such a property can be reduced to proving a simpler one, (in the typical form of Hennessy-Milner logic [HM85]), on the abstract reduced system. The relevant modalities may often be interpreted on the reduced systems, as formulae to check are quite regular. In any case, introduction of a restricted version of modalities in the shape of the partial specifications to check may be obtained using so-called modal specifications [LT88].

We can note that also the expression of properties as constraints on the specification in a constraint oriented style [B89] can be considered as an instance of the use of partial process specification.

### 3.1.3 Use of partial properties

#### Verification and analysis

Partial properties can be used as "commitments" for the implementation, serving as guidelines for the transformation from the specification to an implementation. It should be verified that each refinement step satisfies the commitments. On the other hand, the partial properties satisfied by a LOTOS specification can be derived from the specification itself. Derived properties provide a different view, usually more abstract and less implementation oriented, of the specified system; they can be used to produce assertions that provide a more readable view for a user who is not concerned about architectural details.

A particular case of specification analysis is debugging: deriving a partial view (a "reduction") from a LOTOS specification is promising as a way of checking partial correctness and actually

debugging a LOTOS program under development. Instead of formalising an assertion on the system, it can be derived directly. The synthesized property may sometimes be different from that expected; such a case will suggest misconceptions in the process under analysis, and is a starting point for a diagnostics. This is after all what partial verification should provide, in the absence of total verifications insuring error-free program derivations.

Moreover, we should note that there are classes of typical properties that can be requested of a system and which cannot be expressed directly in LOTOS terms: fairness, divergence, or dually the computation progress (the necessary occurrence of events). Two possible ways of relating these properties to LOTOS specifications are the following:

- 1) Assertions can be used to give additional constraints to the process structure, in order to express properties of this class, so that existing specifications are "enriched" by additional property expressions; this case may also be seen as an extension of the specification language
- 2) It is possible to verify that, under certain constraints, a given LOTOS specification will satisfy given properties which are not expressible in LOTOS terms: for instance, we can verify that, when assuming some general fairness constraints which are not expressed in the specification, a particular response property is satisfied.

### Techniques to achieve verification/derivation of partial properties.

Modal Characterization [HM85] and Temporal Semantics [P81, B87a] provide ways to deduce a logic characterization of the properties enjoyed by a system starting from its LOTOS specification. Once a logic formula representing the behaviour of the system has been obtained, the proof that the system satisfies a given property is reduced to verifying that the formula implies the logic expression of the property itself. Logical deduction can therefore be used both to derive and to verify properties of a given specification.

The equivalent to logical deduction when properties are expressed by process expressions is abstraction: we can derive a partial view of a LOTOS specification by basing the various ways to perform reductions (which could be called transition system "morphisms") on the syntactic notions of abstractions, in which new "abstract" actions are devised, each as a language of sequences of more concrete actions. This can also be viewed also as a way of specifying (and not *programming*) some levels of granularity with respect to the atomicity of sequences of actions. Abstraction can be seen therefore as a transformation changing the atomicity level; the notion of correctness preserved by this transformation is a bisimulation relation, parameterised by the set of actions from which one wants to abstract.

The model checking approach considers transition systems as suitable models of a temporal logic; thus, verifying that a LOTOS specification  $P$  satisfies a property expressed by the temporal logic formula  $F$  amounts to checking that the transition system associated by the operational semantics to  $P$  is a model for  $F$ . This approach, which is suited for property verification, can be supported by automatic tools which perform checking on finite transition systems [CES86].

## 3.1.4 The scope of the present chapter

The explicit, formal definition of the partial properties of LOTOS specifications represents a powerful tool for their analysis. For example, partial properties can be useful to compare LOTOS specifications using non-constructive relations (comparing two specifications by comparing their set of partial properties). In this sense, they are extremely useful to formally

define the "correctness preserving relation"  $R_{CP}$  used in the context of correctness preserving transformation as shown in chapter 1. It should be noted that, since partial properties are usually given at a higher abstraction level than LOTOS specifications, this principle extends to the case of "non LOTOS to LOTOS" and "LOTOS to non LOTOS" transformations, where the lack of any equivalence concepts inhibits any formal reasoning on correctness preservation.

An important subcase of transformations in which partial properties can play an important role is the case of style transformation. Particular properties may be associated with specific styles, while interesting properties to be preserved in the transformation should be independent of the style.

We want to mention the relations of partial properties with formal methods for testing, studied within the Task 1.3: in fact, the acceptance or rejection of a test is a partial property. The expression of tests can be seen as related to the description of partial properties by process expressions.

Three different approaches, which cover the theme of partial properties, are presented in this chapter, each in one of the next three sections.

The first approach aims to relate the LOTOS world to the temporal logic world, defining a Temporal Semantics for Basic LOTOS, that is, a function defined compositionally on the Basic LOTOS terms, which gives the temporal logic formula associated to a LOTOS term (Section 3.2). Some verification examples achieved by relating the Temporal Semantics of some processes to formulae expressing desired properties are shown. Anyway, this approach is particularly promising as an analysis tool of the LOTOS language itself.

The second approach aims to pursue the verification of partial properties by first performing a reduction (imposing a "view" of the system at hand) and then reasoning with temporal logic model checking (Section 3.3). The approach is mainly aimed at obtaining an "explanatory model" of the transition system (associated with a LOTOS specification) with respect to a set of partial properties expressed in temporal logic: the explanatory model and the LOTOS specification being semantically compatible with respect to the set of partial properties which has been selected. The compound method is based upon an extensive use of the standard observational equivalence. A new equivalence, the so-called behaviour equivalence, is introduced; its aim is to deal symmetrically with states and events and to take into account livelock problems. Expressivity associated with behaviour equivalence is comparable to that associated with temporal logic CTL (Computation Tree Logic) [CE81, S82].

The third approach is a more general framework for reductions of processes through transition systems, showing how particular syntactic means to set abstraction on behaviours can produce powerful reductions (Section 3.4). In this approach the accent is posed on the use of reduction principles for debugging LOTOS specifications.

The three approaches employ different constraints on the LOTOS specifications that can be handled, in order to effectively achieve early meaningful results: Temporal Semantics is given for Basic LOTOS, in order to avoid the complexities of the treatment of values, and in the present version is given consistently with "strong" trace semantics (unobservable actions are treated not differently from observable ones); the other approaches, dealing mainly with transition systems, have less concerns about the language itself, but are forced to consider finite state systems.

Such constraint allow however automatic support of the proposed approaches to be feasible. Even if complete automatic support is out of the scope of this document, some considerations on potential tool support are given in Section 3.5.

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